

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

New meta-analysis features in Stata 18

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Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Introduction

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

New meta-analysis features in Stata 18

- ▶ Meta-analysis for prevalence
 - ▶ Stata's meta suite of commands now supports one-sample binary data, allowing you to estimate an overall proportion or prevalence of a symptom, disease, infection, or some other event
- ▶ Multilevel meta-analysis
 - ▶ You can now perform meta-analysis with effect sizes that are nested within higher-level groupings, such as regions or schools

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Overview

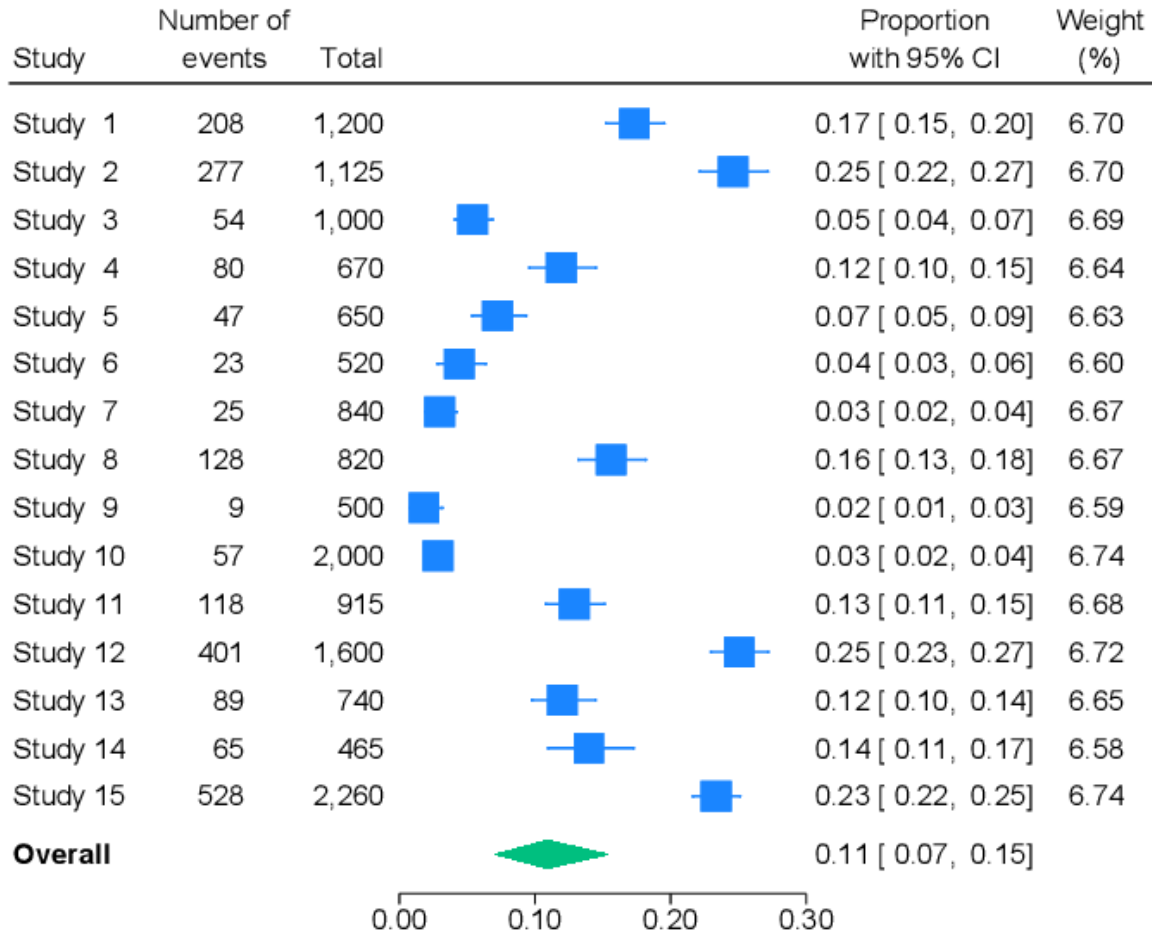
- ▶ Meta-analysis for prevalence
 - ▶ Effect-size computation
 - ▶ Summarizing meta-analysis data
- ▶ Multilevel meta-analysis
 - ▶ Meta-regression
 - ▶ Exploring heterogeneity at different levels
 - ▶ Sensitivity analysis

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

What is meta-analysis?

- ▶ This is a statistical technique for combining the results from several similar studies.
- ▶ The goal is to provide a single estimate of the effect of interest.
- ▶ If results vary widely across studies, the goal is then to understand the inconsistencies in the results.

Chronic kidney disease



Random-effects REML model

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Meta-analysis goals

- ▶ The department of health needs to know the prevalence of chronic kidney disease (CKD) because it is a risk factor for cardiovascular disease
- ▶ Our goal is to report a single estimate of the prevalence of CKD
 - ▶ We assume that the effect sizes are independent across studies.
- ▶ If we observe substantial variation across the studies, we instead focus on trying to explain this variation
- ▶ Perhaps the age of study participants or some other study-level covariates can explain the discrepancies

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Herramientas y procedimientos estadísticos aplicados.

Meta-analysis for prevalence

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Fictional chronic kidney disease (CKD) data

```
. use extremeprop
```

```
. describe
```

Contains data from extremeprop.dta

```
Observations:          15
```

```
Variables:              5
```

```
5 Jul 2023 10:32
```

Variable name	Storage type	Display format	Value label	Variable label
author	str20	%20s		Author
year	float	%9.0g		Year
mean_age	float	%9.0g		Mean age of participants
ssize	float	%9.0g		Sample size
events	float	%9.0g		Number of participants with CKD

Sorted by:

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Meta-analysis data

```
. list author year events ssize
```

	author	year	events	ssize
1.	Ortiz et al.	1975	0	300
2.	Reynolds et al.	2001	1	800
3.	Medina et al.	1980	2	840
4.	Krasinsky et al.	2002	16	520
5.	Cusack et al.	2000	4	105
6.	Kaling et al.	1995	47	650
7.	Johnson et al.	1992	80	670
8.	Villanueva et al.	1992	89	740
9.	Rogen et al.	2004	226	915
10.	Yeun et al.	2008	161	465
11.	Baldwin et al.	2011	348	820
12.	Andrews et al.	2012	72	150
13.	Simone et al.	2007	197	200
14.	Barker et al.	2016	219	220
15.	Young et al.	2004	299	300

Random effects meta-analysis model

K independent studies; each reports the number of events observed and the sample size of the study, allowing us to compute the following:

- ▶ an estimate, $\hat{\theta}_j$, of the true (unknown) effect size θ_j
- ▶ an estimate, $\hat{\sigma}_j$, of its standard error

$$\hat{\theta}_j = \theta + u_j + \epsilon_j$$

for $j = 1, 2, \dots, K$, where $\epsilon_j \sim \mathcal{N}(0, \hat{\sigma}_j^2)$ and $u_j \sim \mathcal{N}(0, \tau^2)$.

The ϵ_j s are the sampling errors and the u_j s are the random effects

- ▶ The estimate of the overall effect size is the mean of the distribution of effect sizes, $\theta_{pop} = \mathbb{E}(\theta_j)$.

Random-effects meta-analysis

- ▶ For each study, we'll compute an estimate of the proportion, $\hat{\theta}_j$, and an estimate, $\hat{\sigma}_j$, of its standard error
- ▶ The overall estimate of the prevalence is a weighted average of the study-specific estimates

$$\hat{\theta}^* = \frac{\sum_{j=1}^K w_j \hat{\theta}_j}{\sum_{j=1}^K w_j}$$

where $w_j = \frac{1}{\hat{\sigma}_j^2 + \hat{\tau}^2}$ and $\hat{\tau}^2$ is the variance of the random effects

Effect sizes for a proportion

Effect size	Estimate	Variance
Raw proportion	$\hat{p} = \frac{e}{n}$	$\frac{\hat{p}(1-\hat{p})}{n}$
Freeman–Tukey	$\hat{p}_{FT} = \arcsin\left(\sqrt{\frac{e}{n+1}}\right) + \arcsin\left(\sqrt{\frac{e+1}{n+1}}\right)$	$\frac{1}{n+0.5}$
Logit	$\text{logit}(\hat{p}) = \ln\left(\frac{\hat{p}}{1-\hat{p}}\right)$	$\frac{1}{n\hat{p}} + \frac{1}{n-n\hat{p}}$

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Summary

- ▶ We are now familiar with
 - ▶ the random-effects meta-analysis model
 - ▶ how the overall estimate is computed (weighted average of the study-specific estimates)
 - ▶ effect sizes for proportions
- ▶ We can now begin working with our data

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Herramientas y procedimientos estadísticos aplicados.

Declare meta-analysis data

```
. meta esize events ssize  
Meta-analysis setting information  
Study information  
  No. of studies: 15  
  Study label: Generic  
  Study size: _meta_studysize  
Summary data: events ssize  
Effect size  
  Type: ftukeyprop  
  Label: Freeman-Tukey's p  
  Variable: _meta_es  
Precision  
  Std. err.: _meta_se  
  CI: [_meta_cil, _meta_ciu]  
  CI level: 95%  
Model and method  
  Model: Random effects  
  Method: REML
```

Contando historias con datos: Herramientas y procedimientos estadísticos aplicados.

System variables

```
. describe
```

Contains data from extremeprop.dta

```
Observations:      15
Variables:         12                    5 Jul 2023 10:32
```

Variable name	Storage type	Display format	Value label	Variable label
author	str20	%20s		Author
year	float	%9.0g		Year
mean_age	float	%9.0g		Mean age of participants
ssize	float	%9.0g		Sample size
events	float	%9.0g		Number of participants with CKD
_meta_id	byte	%9.0g		Study ID
_meta_studylabel	str8	%9s		Study label
_meta_es	double	%10.0g		Freeman-Tukey's p
_meta_se	double	%10.0g		Std. err. for Freeman-Tukey's p
_meta_cil	double	%10.0g		95% lower CI limit for Freeman-Tukey's p
_meta_ciu	double	%10.0g		95% upper CI limit for Freeman-Tukey's p
_meta_studysize	int	%9.0g		Sample size per study

Sorted by:

Note: Dataset has changed since last saved.

Summary of meta-analysis data

```
. meta summarize
```

```
Effect-size label: Freeman-Tukey's p
Effect size: _meta_es
Std. err.: _meta_se
```

```
Meta-analysis summary          Number of studies =    15
Random-effects model          Heterogeneity:
Method: REML                   tau2 =  1.0909
                                I2 (%) =  99.82
                                H2 =  549.89
```

Effect size: Freeman-Tukey's p

Study	Effect size	[95% conf. interval]		% weight
Study 1	0.058	-0.055	0.171	6.66
Study 2	0.085	0.016	0.155	6.68
Study 3	0.109	0.041	0.176	6.68
Study 4	0.358	0.272	0.444	6.67
Study 5	0.414	0.224	0.605	6.63
(output omitted)				
Study 11	1.419	1.351	1.488	6.68
Study 12	1.531	1.371	1.691	6.64
Study 13	2.878	2.739	3.016	6.65
Study 14	2.979	2.847	3.111	6.66
Study 15	3.002	2.889	3.115	6.66
theta	1.139	0.610	1.669	

```
Test of theta = 0: z = 4.01          Prob > |z| = 0.0001
Test of homogeneity: Q = chi2(14) = 5004.80    Prob > Q = 0.0000
```

Summary of meta-analysis data

```
. meta summarize, proportion
```

```
Effect-size label: Freeman-Tukey's p
```

```
Effect size: _meta_es
```

```
Std. err.: _meta_se
```

```
Meta-analysis summary
```

```
Random-effects model
```

```
Method: REML
```

```
Number of studies = 15
```

```
Heterogeneity:
```

```
tau2 = 1.0909
```

```
I2 (%) = 99.82
```

```
H2 = 549.89
```

Study	Proportion	[95% conf. interval]		% weight
Study 1	0.000	0.000	0.006	6.66
Study 2	0.001	0.001	0.005	6.68
Study 3	0.002	0.000	0.007	6.68
Study 4	0.031	0.017	0.048	6.67
Study 5	0.038	0.008	0.085	6.63
(output omitted)				
Study 11	0.424	0.391	0.458	6.68
Study 12	0.480	0.400	0.560	6.64
Study 13	0.985	0.962	0.998	6.65
Study 14	0.995	0.981	0.997	6.66
Study 15	0.997	0.986	0.997	6.66
invftukey(theta)	0.290	0.089	0.549	

```
Test of theta = 0: z = 4.01
```

```
Prob > |z| = 0.0001
```

```
Test of homogeneity: Q = chi2(14) = 5004.80
```

```
Prob > Q = 0.0000
```

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Freeman–Tukey-transformed proportions

- ▶ Freeman–Tukey-transformed proportions have two advantages:
 - ▶ The back-transformed CIs are guaranteed to be in the $[0, 1]$ range
 - ▶ The variance does not depend on the number of events, which means it will not assign artificially large or small weights to studies with \hat{p} close to 0 or 1

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Declare meta-analysis data

► Compute effect sizes

```
meta esize events samplesize [ , model esize(estype) zerocells(spec) ]
```

model: random, common, or fixed

estype: raw proportion, Freeman–Tukey-transformed proportion,
logit-transformed proportion

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Raw proportions

```
. meta esize events ssize, esize(proportion)
```

```
Meta-analysis setting information
```

```
Study information
```

```
  No. of studies: 15
```

```
  Study label: Generic
```

```
  Study size: _meta_studysize
```

```
  Summary data: events ssize
```

```
Effect size
```

```
  Type: proportion
```

```
  Label: Proportion
```

```
  Variable: _meta_es
```

```
Zero-cells adj.: 0.5, only0
```

```
Precision
```

```
  Std. err.: _meta_se
```

```
  CI: [_meta_cil, _meta_ciu]
```

```
  CI level: 95%
```

```
Model and method
```

```
  Model: Random effects
```

```
  Method: REML
```

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Effect sizes for a proportion

Effect size	Estimate	Variance
Raw proportion	$\hat{p} = \frac{e}{n}$	$\frac{\hat{p}(1-\hat{p})}{n}$
Freeman–Tukey	$\hat{p}_{FT} = \arcsin\left(\sqrt{\frac{e}{n+1}}\right) + \arcsin\left(\sqrt{\frac{e+1}{n+1}}\right)$	$\frac{1}{n+0.5}$
Logit	$\text{logit}(\hat{p}) = \ln\left(\frac{\hat{p}}{1-\hat{p}}\right)$	$\frac{1}{n\hat{p}} + \frac{1}{n-n\hat{p}}$

Contando historias con datos: Herramientas y procedimientos estadísticos aplicados.

CI for raw proportions

```
. meta summarize, level(97)
    Effect-size label: Proportion
      Effect size: _meta_es
      Std. err.: _meta_se

Meta-analysis summary
Random-effects model
Method: REML

Number of studies =    15
Heterogeneity:
    tau2 = 0.1435
    I2 (%) = 99.99
    H2 = 9871.81
```

Study	Proportion	[97% conf. interval]		% weight
Study 1	0.002	-0.003	0.007	6.68
Study 2	0.001	-0.001	0.004	6.68
Study 3	0.002	-0.001	0.006	6.68
Study 4	0.031	0.014	0.047	6.68
Study 5	0.038	-0.002	0.079	6.66
(output omitted)				
Study 11	0.424	0.387	0.462	6.66
Study 12	0.480	0.391	0.569	6.60
Study 13	0.985	0.966	1.000	6.67
Study 14	0.995	0.986	1.000	6.68
Study 15	0.997	0.989	1.000	6.68
theta	0.324	0.112	0.536	

```
Test of theta = 0: z = 3.31          Prob > |z| = 0.0009
Test of homogeneity: Q = chi2(14) = 1.3e+05    Prob > Q = 0.0000
```

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Effect sizes for a proportion

- ▶ Logit transformation
 - ▶ Like the Freeman–Tukey transformation, guarantees that back-transformed confidence intervals will be in the $[0, 1]$ range
 - ▶ However, it assigns small weights to studies with \hat{p} close to 0 or 1 for common-effect models
- ▶ Raw proportions
 - ▶ Can produce confidence limits outside the $[0, 1]$ range
 - ▶ Tends to assign large weights to studies with \hat{p} close to 0 or 1 for common-effect models
- ▶ Freeman–Tukey-transformed proportions solve both of these problems; they are variance stabilizing and produce a reasonable CI range

Contando historias con datos: Herramientas y procedimientos estadísticos aplicados.

Fictional CKD data

- ▶ Let's continue with a modified version of the CKD data with less extreme values for the proportions

```
. use myprop1, clear
. list author ssize events mean_age
```

	author	ssize	events	mean_age
1.	Andrews & Thompson	1200	208	37.2
2.	Barker et al.	1125	277	57.4
3.	Cusack & Golds	1000	54	30.1
4.	Johnson & Johnson	670	80	35.3
5.	Kaling et al.	650	47	32.4
6.	Krasinsky & Blunt	520	23	28.2
7.	Medina et al.	840	25	26.5
8.	Ortiz & Baldwin	820	128	36.5
9.	Ortiz et al.	500	9	26.1
10.	Reynolds et al.	2000	57	24.5
11.	Rogen et al.	915	118	36.2
12.	Simone et al.	1600	401	48.6
13.	Villanueva & Blunt	740	89	34.7
14.	Yeun et al.	465	65	37.3
15.	Young et al.	2260	528	62.6

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Computing Freeman–Tukey-transformed proportions

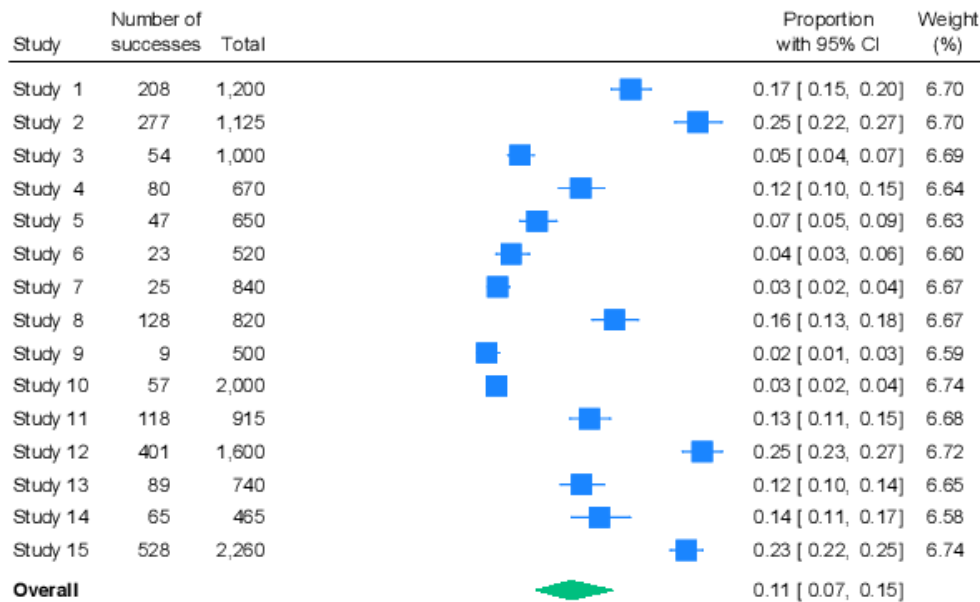
- ▶ Let's compute Freeman–Tukey-transformed proportions

```
. meta esize events ssize
Meta-analysis setting information
Study information
  No. of studies: 15
  Study label: Generic
  Study size: _meta_studysize
  Summary data: events ssize
  Effect size
    Type: ftukeyprop
    Label: Freeman–Tukey's p
    Variable: _meta_es
  Precision
  Std. err.: _meta_se
    CI: [_meta_cil, _meta_ciu]
  CI level: 95%
Model and method
  Model: Random effects
  Method: REML
```

Contando historias con datos: Herramientas y procedimientos estadísticos aplicados.

Forest plot

. meta forestplot, proportion



Heterogeneity: $\tau^2 = 0.07$, $I^2 = 98.53\%$, $H^2 = 67.86$
 Test of $\theta_1 = \theta_2$: $Q(14) = 1136.27$, $p = 0.00$
 Test of $\theta = 0$: $z = 9.50$, $p = 0.00$

Random-effects REML model

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

CIs for individual studies

- ▶ By default, `meta summarize` and `meta forestplot` compute Wald intervals for the proportion of each individual study
- ▶ However, it has been argued that the coverage probability of the Wald interval does not meet the nominal level for extreme values of the proportion and for small sample sizes

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

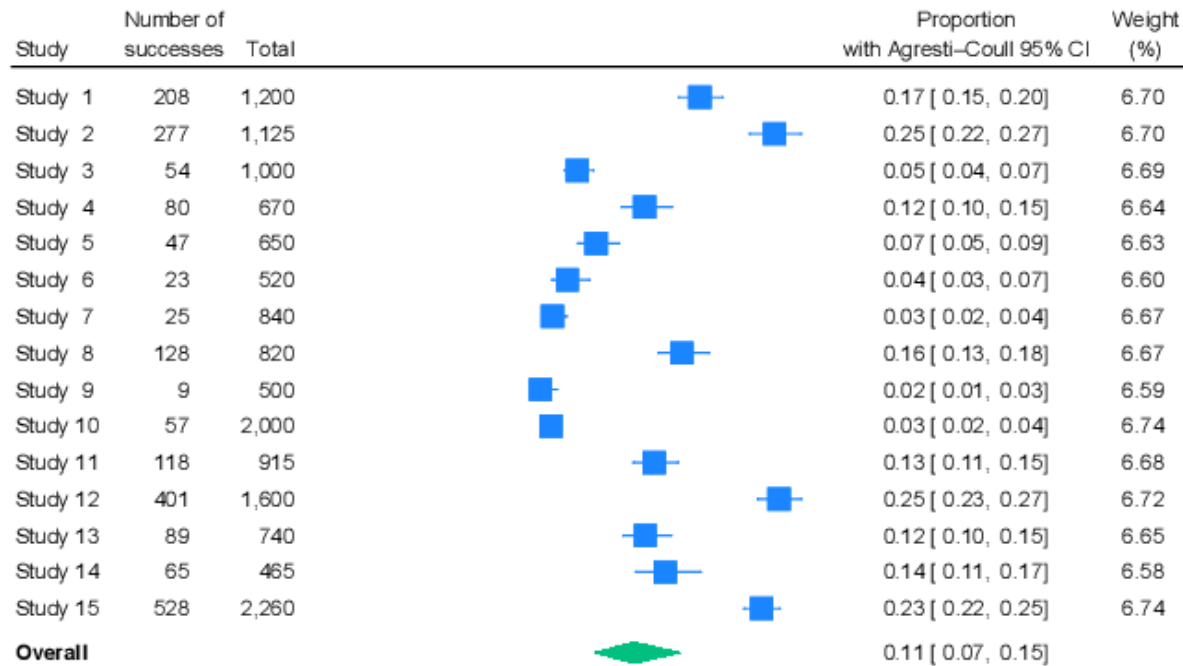
Alternative CIs for individual studies

- ▶ Alternative CI computations include the Clopper–Pearson, Wilson, Agresti–Coull, and Jeffreys and can be obtained with the `citype()` option
- ▶ Brown, Cai, and DasGupta (2001) recommend either the Wilson or Jeffreys interval for a sample size of 40 or less
- ▶ For sample sizes greater than 40, they found the Wilson, Jeffreys, and Agresti–Coull intervals to behave similarly

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Forest plot with alternative CI

. meta forestplot, proportion citype(agresti)



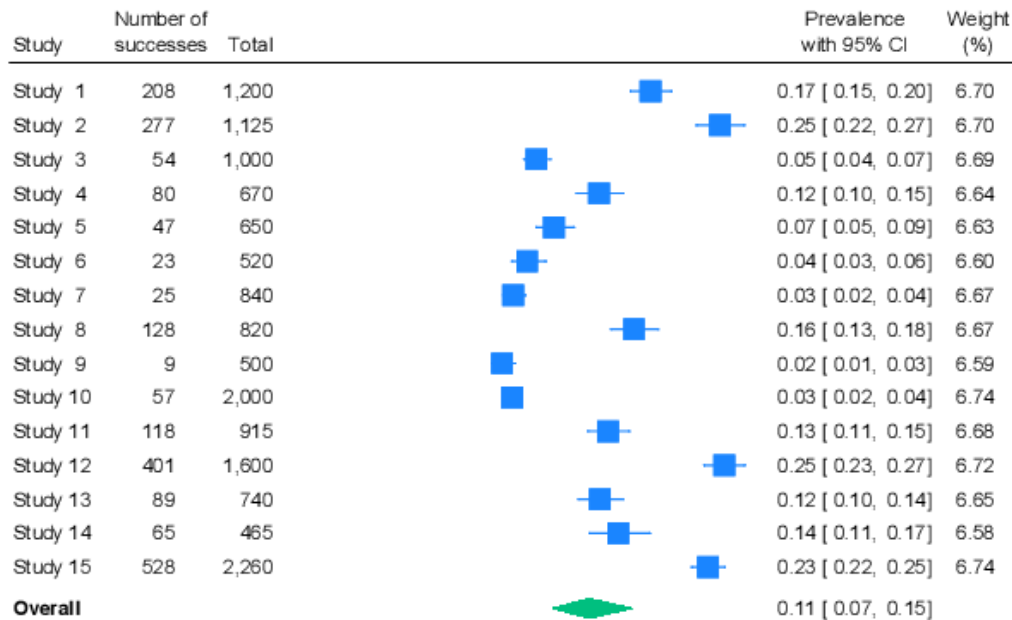
Heterogeneity: $\tau^2 = 0.07$, $I^2 = 98.53\%$, $H^2 = 67.86$
 Test of $\theta_1 = \theta_2$: $Q(14) = 1136.27$, $p = 0.00$
 Test of $\theta = 0$: $z = 9.50$, $p = 0.00$

Random-effects REML model

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Customizing the forest plot

. meta forestplot, prevalence

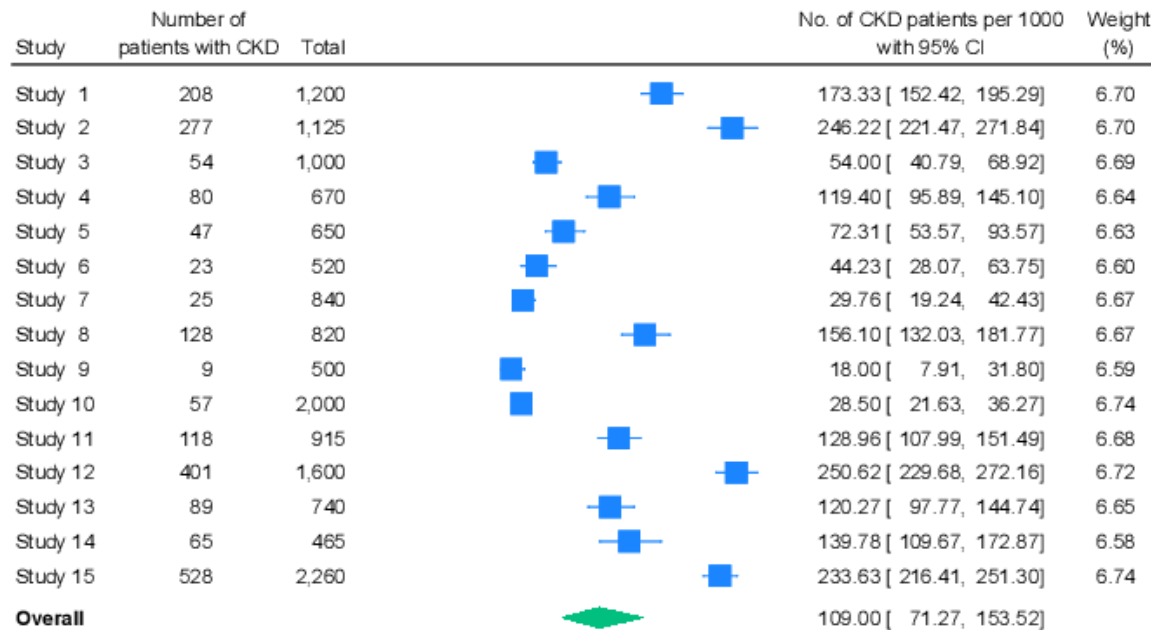


Heterogeneity: $\tau^2 = 0.07$, $I^2 = 98.53\%$, $H^2 = 67.86$
 Test of $\theta = \theta_0$: $Q(14) = 1136.27$, $p = 0.00$
 Test of $\theta = 0$: $z = 9.50$, $p = 0.00$

Random-effects REML model

Customizing the forest plot

```
. meta forestplot, columnopts(_e, title("patients with CKD"))
transform("No. of CKD patients per 1000": invftukey, scale(1000))
```



Heterogeneity: $\tau^2 = 0.07$, $I^2 = 98.53\%$, $H^2 = 67.86$
 Test of $\theta = \theta_0$: $Q(14) = 1136.27$, $p = 0.00$
 Test of $\theta = 0$: $z = 9.50$, $p = 0.00$

Random-effects REML model

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Prediction interval

- ▶ In addition to the CI for the estimate of the overall proportion, we can also compute the prediction interval
- ▶ The prediction interval estimates a plausible range for the proportion in a future study by incorporating the uncertainty of the between-study variance

Prediction interval and Agresti–Coul CI

```
. meta summarize, proportion cotype(agresti) predinterval
```

```
Effect-size label: Freeman–Tukey’s p
```

```
Effect size: _meta_es
```

```
Std. err.: _meta_se
```

```
Meta-analysis summary
```

```
Number of studies = 15
```

```
Random-effects model
```

```
Heterogeneity:
```

```
Method: REML
```

```
tau2 = 0.0668
```

```
I2 (%) = 98.53
```

```
H2 = 67.86
```

Study	Proportion	Agresti–Coul [95% conf. interval]		% weight
Study 1	0.173	0.153	0.196	6.70
Study 2	0.246	0.222	0.272	6.70
Study 3	0.054	0.042	0.070	6.69
Study 4	0.119	0.097	0.146	6.64
Study 5	0.072	0.055	0.095	6.63
(output omitted)				
Study 11	0.129	0.109	0.152	6.68
Study 12	0.251	0.230	0.272	6.72
Study 13	0.120	0.099	0.146	6.65
Study 14	0.140	0.111	0.174	6.58
Study 15	0.234	0.217	0.252	6.74
invftukey(theta)	0.109	0.071	0.154	

Note: Agresti CIs are reported only for individual studies.

95% prediction interval for invftukey(theta): [0.002, 0.343]

Test of theta = 0: z = 9.50

Prob > |z| = 0.0000

Test of homogeneity: Q = chi2(14) = 1136.27

Prob > Q = 0.0000

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Exploring heterogeneity

- ▶ With `meta summarize` we can estimate the overall proportion and with `meta forestplot` we can see how effect sizes vary around the overall estimate
- ▶ We can also perform meta-regression to investigate whether between-study heterogeneity can be explained by one or more moderators

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Random-effects meta-regression

Random-effects meta-regression model:

$$\hat{\theta}_j = x_j\beta + \epsilon_j^* = x_j\beta + u_j + \epsilon_j$$

where $\epsilon_j^* \sim \mathcal{N}(0, \hat{\sigma}_j^2 + \tau^2)$

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Meta-regression

```
. meta regress mean_age
    Effect-size label: Freeman-Tukey's p
      Effect size: _meta_es
      Std. err.: _meta_se
```

Random-effects meta-regression
Method: REML

Number of obs = 15
Residual heterogeneity:
tau2 = .01087
I2 (%) = 91.14
H2 = 11.28
R-squared (%) = 83.72
Wald chi2(1) = 66.74
Prob > chi2 = 0.0000

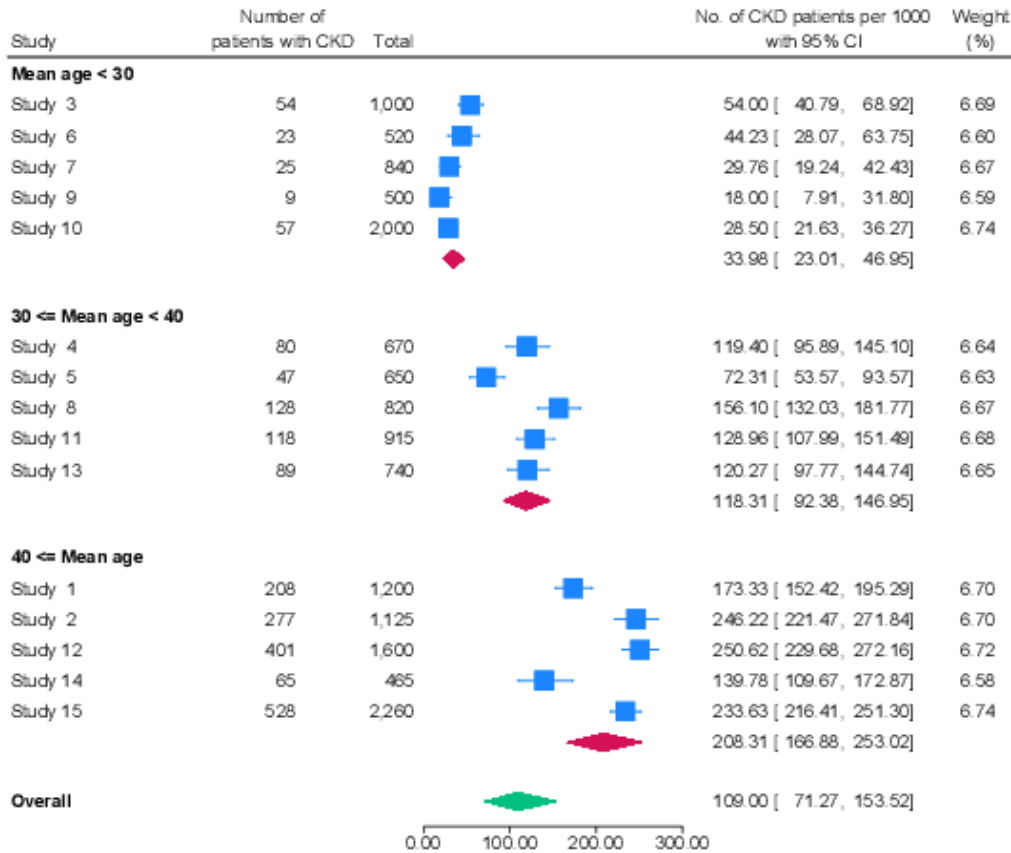
_meta_es	Coefficient	Std. err.	z	P> z	[95% conf. interval]	
mean_age	.0208473	.0025518	8.17	0.000	.0158459	.0258487
_cons	-.1068683	.1001801	-1.07	0.286	-.3032177	.0894812

Test of residual homogeneity: Q_res = chi2(13) = 179.99 Prob > Q_res = 0.0000

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Subgroup-analysis forest plot

. meta forestplot, proportion subgroup(agegroup) ...



Random-effects REML model

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Subgroup meta-analysis

```
. meta summarize, subgroup(agegroup) prop noheader nometashow
(output omitted)
```

Heterogeneity summary

Group	df	Q	P > Q	tau2	% I2	H2
Mean age < 30	4	18.40	0.001	0.004	79.43	4.86
30 <= Mean ~40	4	26.68	0.000	0.008	85.69	6.99
40 <= Mean age	4	51.69	0.000	0.014	94.54	18.31
Overall	14	1136.27	0.000	0.067	98.53	67.86

Test of group differences: $Q_b = \text{chi2}(2) = 92.60$

Prob > $Q_b = 0.000$

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Multilevel meta-analysis

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Multilevel data

- ▶ In our previous example, we performed a standard random-effects meta-analysis in which we assumed that the effect sizes were independent across studies
- ▶ However, if your data have a multilevel (hierarchical) structure, you can perform multilevel meta-analysis to account for the correlation between effect sizes in the same group

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

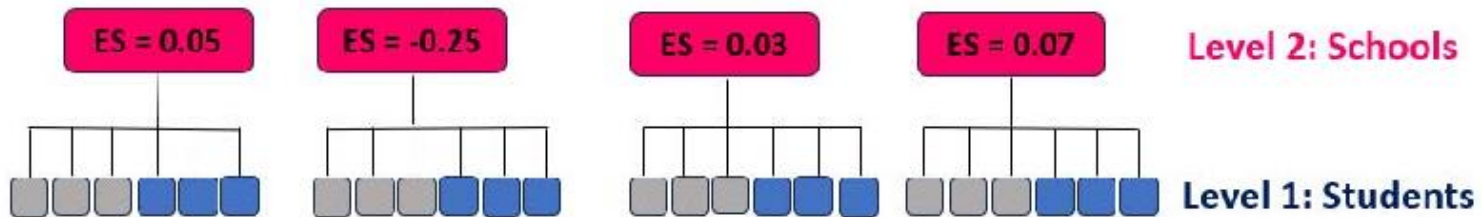
Standard meta-analysis as a two-level model

- ▶ Consider a series of studies that examined whether students performed better under a modified school calendar, with frequent breaks, as opposed to the traditional schedule (Cooper et al. 2003).
- ▶ Each study was performed in a different school
- ▶ The effect size is the standardized mean difference in performance, with positive values indicating that students on the modified calendar performed better than students on the traditional calendar

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Standard meta-analysis as a two-level model

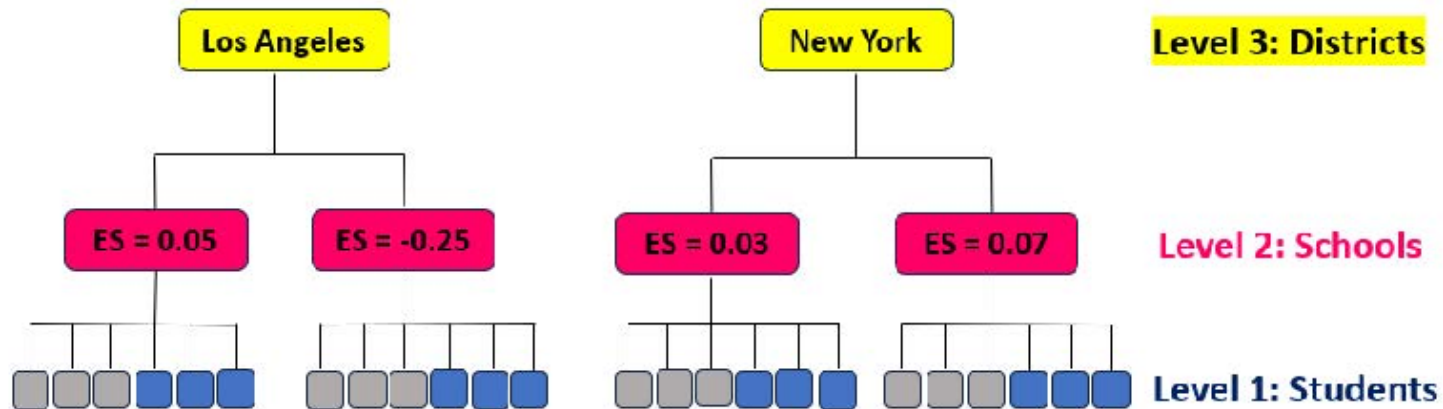
- ▶ Here we see the effect size reported by each study



Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Three-level model

- ▶ Now suppose that multiple studies belong to the same district
- ▶ Schools belonging to the same district will be more similar in terms of demographics and socioeconomical factors, resulting in a correlation between results within a district



- ▶ Here we see how studies are grouped by district

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Modified school calendar data

```
. use schoolcal2, clear
(Effect of modified school calendar on student achievement)
. describe
Contains data from schoolcal2.dta
Observations:      56          Effect of modified school calendar on student achievement
Variables:         9           5 Jul 2023 11:06
                          (_dta has notes)
```

Variable name	Storage type	Display format	Value label	Variable label
district	int	%12.0g		District ID
school	byte	%9.0g		School ID
study	byte	%12.0g		Study ID
stdmdiff	double	%10.0g		Standardized difference in means of achievement test scores
var	double	%10.0g		Within-study variance of stdmdiff
year	int	%12.0g		Year of the study
se	double	%10.0g		Within-study standard-error of stdmdiff
year_c	byte	%9.0g		Year of the study centered around 1990
mean_exp	float	%9.0g		Mean teacher experience

Sorted by: district

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Modified school calendar data

```
. list district school study stdmdiff mean_exp in 1/11, sepby(district)
```

	district	school	study	stdmdiff	mean_exp
1.	11	1	1	-.18	6.394918
2.	11	2	2	-.22	1.820014
3.	11	3	3	.23	7.86858
4.	11	4	4	-.3	8.369441
5.	12	1	5	.13	10.48499
6.	12	2	6	-.26	10.73829
7.	12	3	7	.19	2.892403
8.	12	4	8	.32	6.689758
9.	18	1	9	.45	5.5483
10.	18	2	10	.38	13.40538
11.	18	3	11	.29	3.927117

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Multilevel meta-analysis model

By performing a multilevel meta-analysis, we can

- ▶ estimate the effect size more precisely by accounting for the dependence between observations within a group
- ▶ assess the heterogeneity between schools within a district and between districts
- ▶ estimate how each district varies from the overall mean
 - ▶ This will help us decide whether the modified calendar should be applied to some districts and not others

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Multilevel meta-analysis model

We'll fit a three-level random-intercepts model

$$\hat{\theta}_{jk} = \theta + u_j^{(3)} + u_{jk}^{(2)} + \epsilon_{jk}$$

where $u_j^{(3)} \sim \mathcal{N}(0, \tau_3^2)$, $u_{jk}^{(2)} \sim \mathcal{N}(0, \tau_2^2)$, and $\epsilon_{jk} \sim \mathcal{N}(0, \hat{\sigma}_{jk}^2)$. Note that j represents the third level (district), k represents the second level (school within district), and ϵ_{jk} represents the sampling errors.

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Three-level meta-analysis

```
. meta multilevel stdmdiff, relevels(district school) essevariable(se) nolog
Multilevel REML meta-analysis                               Number of obs = 56
```

Grouping information

Group variable	No. of groups	Observations per group		
		Minimum	Average	Maximum
district	11	3	5.1	11
school	56	1	1.0	1

```
Log restricted-likelihood = -7.9587239
Wald chi2(0) = .
Prob > chi2 = .
```

stdmdiff	Coefficient	Std. err.	z	P> z	[95% conf. interval]	
_cons	.1847132	.0845559	2.18	0.029	.0189866	.3504397

```
Test of homogeneity: Q_M = chi2(55) = 578.86
Prob > Q_M = 0.0000
```

Random-effects parameters	Estimate
district: Identity	
sd(_cons)	.2550724
school: Identity	
sd(_cons)	.1809324

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Assess variability among effect sizes

```
. estat heterogeneity
```

```
Method: Cochran
```

```
Joint:
```

```
I2 (%) = 90.50
```

```
Method: Higgins–Thompson
```

```
district:
```

```
I2 (%) = 63.32
```

```
school:
```

```
I2 (%) = 31.86
```

```
Total:
```

```
I2 (%) = 95.19
```

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Fit a two-level model

- ▶ We want to test whether there is a nonnegligible amount of heterogeneity between the schools within a district
- ▶ First, we store our results from the previous model

```
. meta multilevel stdmdiff, ///  
  relevels(district school) essevariable(se)  
. estimates store full_model
```

- ▶ We now fit a two-level model with district as the second level

```
. meta multilevel stdmdiff, ///  
  relevels(district) essevariable(se)  
. estimates store district effect
```

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Likelihood-ratio test

```
. lrtest full_model district_effect  
Likelihood-ratio test  
Assumption: district_eff~t nested within full_model  
LR chi2(1) = 48.52  
Prob > chi2 = 0.0000
```

Note: The reported degrees of freedom assumes the null hypothesis is not on the boundary of the parameter space. If this is not true, then the reported test is conservative.

Note: LR tests based on REML are valid only when the fixed-effects specification is identical for both models.

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Sensitivity analysis

- ▶ Suppose we're interested in exploring how different magnitudes of the school-level variation impact our estimates of the overall standardized mean difference and the district-level variation
- ▶ To answer this question, we'll refit our model, each time setting the random-effects standard deviations for the school level to a different value

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Random-intercepts standard deviations

```
. meta multilevel stdmdiff, ///  
  relevels(district school, sd(. 0.01)) esse(se)  
. estimates store fixsd1  
. meta multilevel stdmdiff, ///  
  relevels(district school, sd(. 0.18)) esse(se)  
. estimates store fixsd2  
. meta multilevel stdmdiff, ///  
  relevels(district school, sd(. 0.60)) esse(se)  
. estimates store fixsd3
```

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Comparing effect sizes

```
. estimates table _all, stats(sd2) keep(stdmdiff:_cons) b(%8.3f) se(%8.3f)
```

Variable	fixsd1	fixsd2	fixsd3
_cons	0.196	0.185	0.123
	0.090	0.085	0.083
sd2	0.010	0.180	0.600

Legend: b/se

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Comparing random-effects standard deviations for districts

```
. estimates table _all, stats(sd2) keep(lns1_1_1:_cons) b(%8.3f) eform
```

Variable	fixsd1	fixsd2	fixsd3
_cons	0.288	0.255	0.000
sd2	0.010	0.180	0.600

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

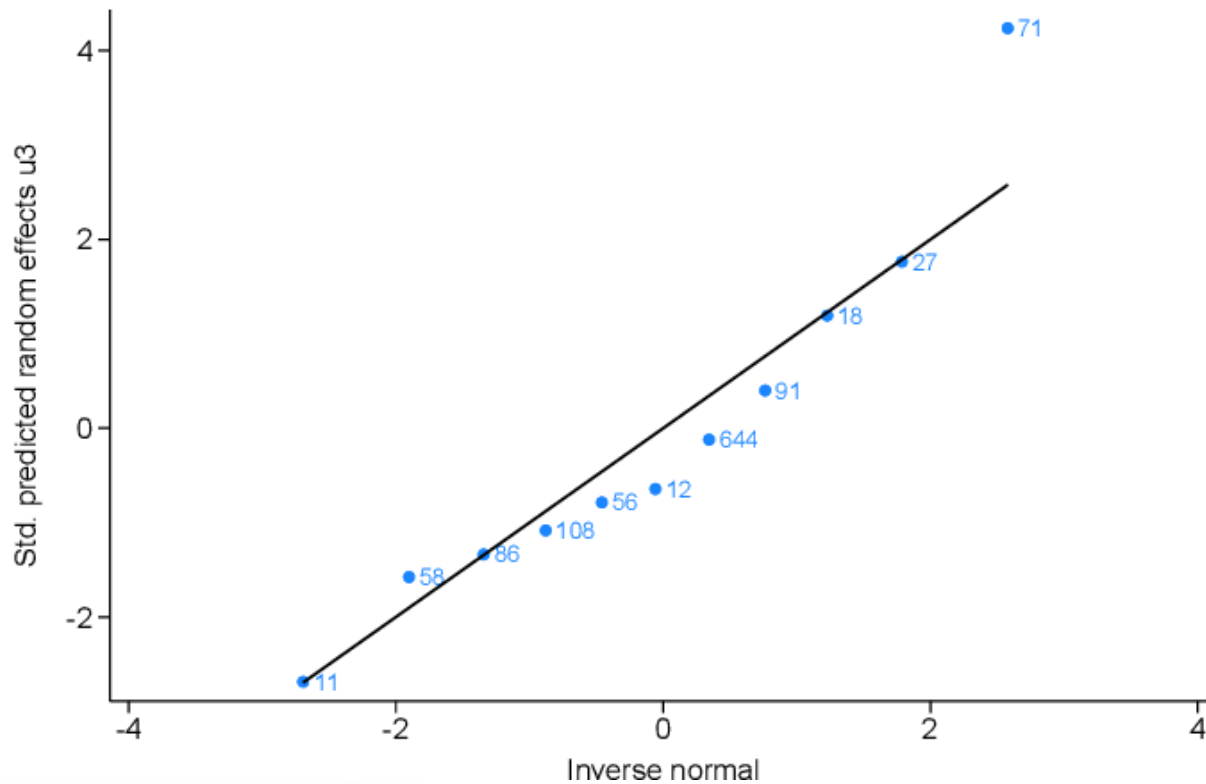
Predictions of random effects

```
. qui: meta multilevel stdmdiff, relevels(district school) esse(se)
. predict double u3 u2, reffects reses(se_u3 se_u2, diagnostic)
. by district, sort: generate tolist = (_n==1)
. list district u3 se_u3 if tolist
```

	district	u3	se_u3
1.	11	-.18998596	.07071817
5.	12	-.08467077	.13168501
9.	18	.1407273	.11790486
12.	27	.24064814	.13641505
16.	56	-.1072942	.13633364
20.	58	-.23650899	.15003184
31.	71	.53427781	.12606072
34.	86	-.2004695	.1499012
42.	91	.05711692	.14284823
48.	108	-.14168396	.13094894
53.	644	-.01215679	.10054689

Normal quantile plot

- . generate double uстан3 = u3/se_u3
- . qnorm uстан3 if tolist, mlabel(district)



Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Models with random slopes

- ▶ `meta multilevel` allows us to fit random-intercepts meta-analysis models

```
. meta multilevel stdmdiff, relevels(district school) esse(se)
```

- ▶ We can also fit this model as follows:

```
. meta meregress stdmdiff || district: || school:, esse(se)
```

- ▶ If we wish to include random slopes, we can instead use `meta meregress`

```
. meta meregress stdmdiff x1 || district: x1 || school:, esse(se)
```

- ▶ The `me` in `meregress` refers to mixed effects

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Three-level meta-regression with random slopes

```
> || district: mean_exp ///
> || school:, essevariable(se) nolog nogroup
```

Multilevel REML meta-regression Number of obs = 56
Wald chi2(1) = 8.37
 Log restricted-likelihood = -3.3635425 Prob > chi2 = 0.0038

stdmdiff	Coefficient	Std. err.	z	P> z	[95% conf. interval]	
mean_exp	-.0262054	.009058	-2.89	0.004	-.0439587	-.0084521
_cons	.3580009	.0981127	3.65	0.000	.1657036	.5502982

Test of homogeneity: Q_M = chi2(54) = 558.47 Prob > Q_M = 0.0000

Random-effects parameters	Estimate
district: Independent	
sd(mean_exp)	.0156308
sd(_cons)	.2605429
school: Identity	
sd(_cons)	.146955

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Display variance components

```
. estat sd, variance
```

Random-effects parameters	Estimate
district: Independent	
var(mean_exp)	.0002443
var(_cons)	.0678826
school: Identity	
var(_cons)	.0215958

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Conclusion

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Summary

- ▶ Today, we learned how to do the following in Stata:
 - ▶ Compute different effect sizes for meta-analysis of prevalence.
 - ▶ Summarize meta-analysis data in both a table and a graph.
 - ▶ Perform meta-regression with effect sizes that have hierarchical structures.
 - ▶ Assess heterogeneity at different levels of the hierarchy.

Contando historias con datos:
Herramientas y procedimientos estadísticos aplicados.

Resources

- ▶ Overview of **meta-analysis features** in Stata
- ▶ Video tutorial on **performing meta-analysis in Stata**
- ▶ *Stata Meta-Analysis Reference Manual*

Contando historias con datos: Herramientas y procedimientos estadísticos aplicados.

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