

Description	Syntax	Remarks and examples	Conformability
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Description

`_invmat(A)` and `_invmat(A, tol)` overwrite the original real or complex, square matrix *A* with the inverse of *A* if *A* has full rank and with the Moore–Penrose pseudoinverse if not. The function returns a real scalar 0 if the inverse is computed and 1 if the pseudoinverse is computed.

The optional argument *tol* specifies the tolerance for determining singularity; see [Remarks and examples](#) below.

Syntax

real scalar `_invmat(numeric matrix A)`

real scalar `_invmat(numeric matrix A, real scalar tol)`

Remarks and examples

These routines calculate the inverse of *A* if *A* has full rank. The inverse matrix A^{-1} of *A* satisfies the conditions

$$AA^{-1} = I$$

$$A^{-1}A = I$$

A is required to be square.

However, if *A* is singular or close to singular, the Moore–Penrose pseudoinverse is computed instead. The Moore–Penrose pseudoinverse is also known as the Moore–Penrose inverse and as the generalized inverse.

The pseudoinverse A^* of *A* satisfies four conditions,

$$A(A^*)A = A$$

$$(A^*)A(A^*) = A^*$$

$$(AA^*)' = A(A^*)$$

$$(A^*A)' = (A^*)A$$

where the transpose operator $'$ is understood to mean the conjugate transpose when *A* is complex. Also, if *A* is of full rank, then

$$A^* = A^{-1}$$

See [M-5] [pinv\(\)](#) for details about pseudoinverse.

▷ Example 1: Full-rank matrix

If A has full rank, the function returns 0 and computes the inverse. Here we compute the inverse and show that $AA^{-1} = I$.

```
: A
      1      2      3
1      1      2      3
2     2.5      5      1
3      3      2      1

: rc = _invmat(Ainv = A)
: rc
0

: Ainv
      1      2      3
1    -0.1153846154  -0.1538461538      0.5
2    -0.0192307692   0.3076923077  -0.25
3     0.3846153846  -0.1538461538      0

: Ainv * A
      1      2      3
1      1    -2.22045e-16  -1.11022e-16
2    1.11022e-16      1    2.77556e-17
3      0      0      1
```

You may verify other conditions for the inverse yourself.



▷ Example 2: Singular matrix

If B does not have full rank, the function returns 1 and computes the pseudoinverse. Here we compute the pseudoinverse and show that $B(B^*)B = B$ and $(B^*)B(B^*) = B^*$.

```
: B
      1      2
1      1      2
2      0      0

: rc = _invmat(Binv = B)
: rc
1

: Binv
      1      2
1     0.2      0
2     0.4      0
```

```
: mreldif(B * Binv * B, B), mreldif(Binv * B * Binv, Binv)
      1                2
1 [ 0  3.96508e-17 ]
```

You may verify other conditions for the pseudoinverse yourself.



Conformability

`_invmat(A, tol)`:

input:

A : $n \times n$
 tol : 1×1 (optional)

output:

A : $n \times n$
result: 1×1

Diagnostics

The inverse returned by these functions is real if A is real and is complex if A is complex. The determination of singularity is made relative to tol . See [Tolerance](#) under *Remarks and examples* in [\[M-5\] lusolve\(\)](#) for details.

`_invmat(A)` returns a matrix containing missing if A contains missing values.

`_invmat(A)` aborts with error if A is a view.

See [\[M-5\] lusolve\(\)](#) and [\[M-1\] Tolerance](#) for information on the optional tol argument.

References

Moore, E. H. 1920. On the reciprocal of the general algebraic matrix. *Bulletin of the American Mathematical Society* 26: 394–395.

Penrose, R. 1955. A generalized inverse for matrices. *Mathematical Proceedings of the Cambridge Philosophical Society* 51: 406–413. <https://doi.org/10.1017/S0305004100030401>.

Also see

- [M-5] [cholinv\(\)](#) — Symmetric, positive-definite matrix inversion
- [M-5] [invsym\(\)](#) — Symmetric real matrix inversion
- [M-5] [luinv\(\)](#) — Square matrix inversion
- [M-5] [pinv\(\)](#) — Moore–Penrose pseudoinverse
- [M-5] [qrinv\(\)](#) — Generalized inverse of matrix via QR decomposition
- [M-5] [_solveamat\(\)](#) — Solve $AX=B$ for X
- [M-4] [Matrix](#) — Matrix functions
- [M-4] [Solvers](#) — Functions to solve $AX=B$ and to obtain A inverse

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