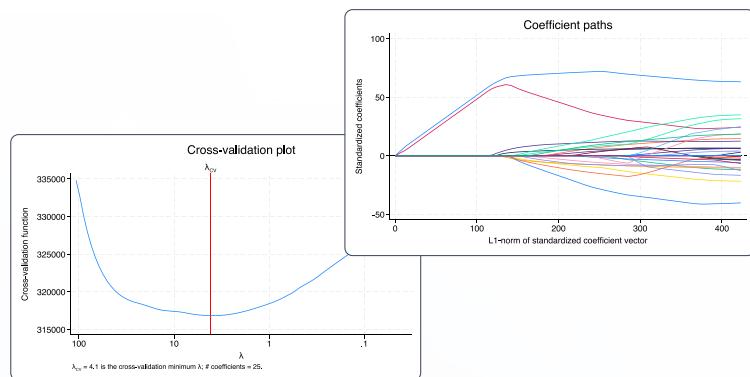


# Lasso

## Variable selection, prediction, inference



- All the tools you expect for lasso machine learning
  - Lasso, square-root lasso, and elastic net
  - Cross-validation
  - Adaptive lasso
  - Knot analysis
  - Coefficient paths
  - Adjustment for clustered data

- Alongside cutting-edge inferential methods
  - Robust to mistakes in variable selection
  - Proper inference for coefficients of interest
  - Double selection
  - Partialing out
  - Cross-fit partialing out
  - Double machine learning
  - Treatment-effects estimation
  - Inference for clustered data

### Select predictors for continuous, binary, count, and survival-time **New** outcomes

Lasso with selection via cross-validation

```
. lasso linear y x1-x1000
. lasso logit y x1-x1000
. lasso probit y x1-x1000
. lasso poisson y x1-x1000
. lasso cox x1-x1000
```

Adaptive lasso

```
. lasso linear y x1-x1000, selection(adaptive)
```

Selection via BIC

```
. lasso linear y x1-x1000, selection(bic)
```

Selection via plugin method

```
. lasso linear y x1-x1000, selection(plugin)
```

Elastic net with selection via cross-validation

```
. elasticnet linear y x1-x1000
. elasticnet logit y x1-x1000
. elasticnet probit y x1-x1000
. elasticnet poisson y x1-x1000
. elasticnet cox x1-x1000
```

Square-root lasso

```
. sqrllasso y x1-x1000
```

### Examine the results

View selected variables

```
. lassoknots
. lassoinfo
. lassocoef
```

Obtain predictions

```
. use newdata
. predict yhat
```

Plot cross-validation function

```
. cvplot
```

Evaluate fit

```
. lassogof
```

Plot coefficient path

```
. coefpath
```

| Viewer - view lasso1.smcl              |                 |                             |                      |                         |                          |
|--|-----------------|-----------------------------|----------------------|-------------------------|--------------------------|
| view lasso1.smcl X                     |                 |                             |                      |                         |                          |
| + Dialog Also see Jump to              |                 |                             |                      |                         |                          |
| <pre>. lasso linear y x1-x10</pre>     |                 |                             |                      |                         |                          |
|  |                 | No. of obs                  | =                    | 69                      |                          |
|  |                 | No. of covariates           | =                    | 10                      |                          |
|  |                 | Selection: Cross-validation |                      | No. of CV folds         | = 10                     |
| ID                                     | Description     | lambda                      | No. of nonzero coef. | Out-of-sample R-squared | CV mean prediction error |
| 1                                      | first lambda    | 4.69114                     | 0                    | -0.0090                 | 34.22157                 |
| 17                                     | lambda before   | 1.0588                      | 3                    | 0.5641                  | 14.78393                 |
| * 18                                   | selected lambda | .9647388                    | 3                    | 0.5648                  | 14.76141                 |
| 19                                     | lambda after    | .8790341                    | 3                    | 0.5645                  | 14.77163                 |
| 22                                     | last lambda     | .664957                     | 5                    | 0.5613                  | 14.87944                 |
| * lambda selected by cross-validation. |                 |                             |                      |                         |                          |
| <pre>. estimates store cv</pre>        |                 |                             |                      |                         |                          |
| <pre>. lassocoef cv adaptive</pre>     |                 |                             |                      |                         |                          |
|  |                 | cv                          | adaptive             |                         |                          |
| x5                                     | x               | x                           |                      |                         |                          |
| x6                                     | x               | x                           |                      |                         |                          |
| x7                                     | x               |                             |                      |                         |                          |
| _cons                                  | x               | x                           |                      |                         |                          |

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# Lasso for inference

With lasso inferential methods, you can estimate coefficients, standard errors, test statistics, and confidence intervals for variables of interest while using lassos to select from a potentially large number of control variables.

Double-selection method; estimate coefficients for **x1** and categorical **x2**; selection of controls via plugin

```
. dsregress y x1 i.x2, controls(c1-c1000)
```

Logit model for binary outcome; estimate odds ratios for **x1** and **x2**

```
. dslogit y x1 i.x2, controls(c1-c1000)
```

Poisson model for count outcome; estimate incidence-rate ratios for **x1** and **x2**

```
. dspoisson y x1 i.x2, controls(c1-c1000)
```

Selection of controls via cross-validation

```
. dsregress y x1 i.x2, controls(c1-c1000)  
    selection(cv)
```

Partialing-out method

```
. poregress y x1 i.x2, controls(c1-c1000)
```

Cross-fit partialing-out method (double machine learning)

```
. xporegress y x1 i.x2, controls(c1-c1000)
```

Treatment-effects estimation; estimate the ATE of **treat**, controlling for **x1-x1000** in the outcome model and **w1-w1000** in the treatment model

```
. telasso (y x1-x1000) (treat w1-w1000)
```

| Double-selection linear model |   |             |                  |       |       |                      |
|-------------------------------|---|-------------|------------------|-------|-------|----------------------|
|                               | y | Coefficient | Robust std. err. | z     | P> z  | [95% conf. interval] |
| x1                            |   | .1272712    | .256027          | 0.50  | 0.619 | -.3745326 .629075    |
| x2                            | 2 | .2792513    | 1.270518         | 0.22  | 0.826 | -2.210918 2.76942    |
|                               | 3 | -.2613078   | 1.358118         | -0.19 | 0.847 | -2.92317 2.400554    |
|                               | 4 | .7492284    | 1.427334         | 0.52  | 0.600 | -2.048295 3.546752   |
|                               | 5 | 4.082883    | 1.905783         | 2.14  | 0.032 | .3476163 7.81815     |

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## Evaluate results using Stata's standard tools

Perform tests on coefficients

```
. test x1=1
```

Estimate contrasts such as differences across levels

```
. contrast ar.x2
```

| Contrasts of marginal linear predictions |          |           |                      |           |          |  |
|--|----------|-----------|----------------------|-----------|----------|--|
|  | Contrast | Std. err. | [95% conf. interval] |           |          |  |
| x2                                       | (2 vs 1) | .2792513  | 1.270518             | -2.210918 | 2.76942  |  |
|  | (3 vs 2) | -.5405591 | .8160264             | -2.139941 | 1.058823 |  |
|  | (4 vs 3) | 1.010536  | .8213126             | -.5992068 | 2.620279 |  |
|  | (5 vs 4) | 3.333655  | 2.073229             | -.7297991 | 7.397108 |  |

## Explore underlying lassos

View the selected controls in the lasso for **y**

```
. lassocoef (.,for(y))
```

Plot coefficient paths in the lasso for **y**

```
. coefpath, for(y)
```

