Semiparametric analysis of case–control genetic data in the presence of environmental factors

Yulia Marchenko

Senior Statistician StataCorp LP

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The main goal of genetic disease association studies is to determine the genetic basis for complex diseases. Specifically, the aim is to identify genetic variants which either directly influence complex diseases or are in linkage disequilibrium with such causal variants.

Biallelic SNPs are often used as genetic markers in association studies thanks to availability of high-density SNP maps published by International SNP Map Working Group (2001) and International HapMap Consortium (2003).



Definition

Single nucleotide polymorphism (SNP, pronounced as "snip") is a single nucleotide (A, T, C, or G) variation of the DNA sequence that occurs in at least 1% of the population.

For example, DNA fragments AAGC**C**TA and AAGC**T**TA from two subjects differ in a single nucleotide. In this example, the bases **C** and **T** are referred to as *alleles*, alternative forms of a DNA segment at a single locus.

A ${\rm SNP}$ is often coded as 1 if a rare allele is present at a ${\rm SNP}$ site and 0, otherwise.



Definition

Haplotype is a sequence of closely linked SNPs on the same chromosome within the genomic region of interest. *Diplotype* is a set of two haplotypes humans carry in the pair of homologous chromosomes.

Using binary coding of SNPs, a haplotype can be represented as a binary sequence and a diplotype can be represented as a pair of binary sequences. With M SNP sites (loci), there are 2^M possible haplotypes and 2^{2M} possible diplotypes.

For example, M = 3:

8 possible haplotypes: 000, 001, 010, 011, 100, 101, 110, 111 64 possible diplotypes: (000,000), (000,001), ..., (111,110), (111,111)

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In haplotype-based disease association studies, a subject's genetic information is described by a diplotype. In practice however we usually observe genotypes instead of diplotypes.

Definition

Genotype is a combination of the haplotypes from a pair of homologous chromosomes.

Mathematically speaking, if H_1 and H_2 are two haplotypes (binary sequences), a genotype $G = H_1 + H_2$ is the sum of these two binary sequences resulting in a sequence of the numbers 0, 1, and 2.

In the previous example (M = 3): $3^3 = 27$ possible genotypes: 000, 001, ..., 221, 222



Data from a case-control haplotype-based disease association study usually consist of

- a disease (or case-control) status D = 0, 1;
- genotype data from M tightly linked SNPs $G = (g_1, \ldots, g_M), g_k \in \{0, 1, 2\}$; and
- subjects' characteristics and environmental exposures $X = (x_1, \dots, x_p).$

We consider the case when the data are collected from samples of unrelated individuals using the retrospective sampling scheme.



- select people with D = 1 and sample from them to obtain values of covariates Z;
- select people with D = 0 and sample from them to obtain values of covariates Z;
- samples (covariate values) are obtained conditional on the disease status *D*.



Recall that under the case-control sampling design, the likelihood function

$$f_{Z|D}(z|d) = \frac{\Pr(D = d|Z = z)f_Z(z)}{\Pr(D = d)}$$

depends on the probability of disease $Pr(D = d) = \pi_d$ in the population, the covariate distribution $f_Z()$ in the population, and the likelihood function under the prospective design Pr(D|Z).

Under the considered logistic model,

$$\Pr(D = 1 | Z = z; \alpha_0, \beta) = \mathcal{K}(\alpha_0 + \beta^\top z)$$

where $\mathcal{K}(a) = \exp(a)\{1 + \exp(a)\}^{-1}$ and $\beta = (\beta_1, \dots, \beta_p)^\top$.



Link between prospective and retrospective likelihood functions

Prentice and Pyke (1979) showed that one can obtain MLEs of β by fitting the standard logistic model (ignoring the retrospective design) to case-control data without any parametric assumptions about the covariate distribution $f_Z()$.

Roeder et al. (1996), besides extending the result to the case of covariates measured with error, provided the explicit relationship between the parameters of the prospective and retrospective likelihood functions:

$$\boldsymbol{\beta}^{\star} = \boldsymbol{\beta}$$
 and $\alpha_0^{\star} = \alpha_0 + \log(n_1/n_0) - \log(\pi_1/\pi_0)$

where n_1 and n_0 are the respective numbers of cases and controls.

Note

Intercept α_0 is not estimable from a prospective logistic regression with case-control data unless the probability of a disease in the population π_1 is known.

Semiparametric efficiency of the standard logistic model with case-control data

Breslow et al. (2000) showed that standard logistic regression is semiparametric-efficient (the variance of coefficients attains the lower bound of the underlying semiparametric model) under the case-control sampling design.

Assumption

The semiparametric-efficiency of the prospective-type analysis of case-control data holds under the assumption of an arbitrary covariate distribution.



With SNP genetic data, we want to study the effect of *risk haplotypes* (target haplotypes whose effect on a disease is of interest) on the disease and possibly their interaction with environmental exposures X.

Subjects' genetic information consists of diplotypes, haplotype pairs, $H^{d} = (H_k, H_l)$ with constituent haplotypes H_k and H_l . As such, the effect of risk haplotypes may be modeled according to various genetic models depending on the number of copies of the risk haplotype present in a subject's diplotype.



Haplotype-effects logistic model with risk haplotypes H^* and environmental factors X is

$$\Pr(D = 1 | X, H^{d}; \alpha_{0}, \beta_{X}, \gamma_{H^{\star}}) = K\{\alpha_{0} + \beta_{X}X + m(H^{d}, X; \gamma_{H^{\star}})\}$$

where function $m(H^d, X; \gamma_{H_{\star}})$ is linear in risk haplotype parameters $\gamma_{H^{\star}}$ with coefficients determined by a risk haplotype model (or mode of inheritance).



Modes of inheritance, main effects only

Consider a single risk haplotype H_1^{\star} and its main effect on the disease. In general (under the codominant model),

$$m\{H^{d} = (H_{k}, H_{l}); \gamma_{H_{1}^{\star}}\} = \{I(H_{k} = H_{1}^{\star}) + I(H_{l} = H_{1}^{\star})\}\beta_{H_{1}^{\star}}^{a} + I(H_{k} = H_{l} = H_{1}^{\star})\beta_{H_{1}^{\star}}^{r}$$

where I() denotes the indicator function and $\gamma_{H_1^{\star}} = (\beta_{H_1^{\star}}^a, \beta_{H_1^{\star}}^r)^{\top}$.

- codominant the effects of having two copies of a risk haplotype in a diplotype and a single copy can be different
- additive having two copies of a risk haplotype in a diplotype doubles the effect compared to having only one copy; β^r_{H^{*}} = 0
- **recessive** only having exactly two copies of a risk haplotype has an effect on a disease; $\beta_{H_1^*}^a = 0$

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• dominant – having one or two copies of a risk haplotype has the same effect on a disease; $\beta_{H_1^*}^r = -\beta_{H_1^*}^a$

Recall our earlier example with M = 3 SNP loci.

Subjects' diplotypes: $H_1^d = (000, 111)$, $H_2^d = (010, 100)$, $H_3^d = (010, 010)$ Risk haplotype H_1^\star : 010

Table: Expressions of $m\{H^{d} = (H_k, H_l); \gamma_{H_1^{\star}}\}$ for different diplotypes under four genetic models.

	additive	dominant	recessive	codominant
H_1^{d}	0	0	0	0
$H_2^{ m d}$	$eta^{a}_{H_{1}^{\star}}$	$eta^{a}_{H_{1}^{\star}}$	0	$eta_{H_1^\star}^{a}$
$H_3^{ m d}$	$2eta_{H_1^\star}^{a}$	$\beta_{H_1^\star}^a$	$eta_{\textit{H}_{1}^{\star}}^{\textit{r}}$	$2\beta^{a}_{H_{1}^{\star}}+\beta^{r}_{H_{1}^{\star}}$



Modes of inheritance, interaction

We can add the interaction effect of H_1^{\star} with an environmental factor X_1 . Then, under the codominant model,

$$\begin{split} m(H^{d}, X_{1}; \gamma_{H_{1}^{\star}}) &= \{I(H_{k} = H_{1}^{\star}) + I(H_{l} = H_{1}^{\star})\}\beta_{H_{1}^{\star}}^{a} \\ &+ I(H_{k} = H_{l} = H_{1}^{\star})\beta_{H_{1}^{\star}}^{r} \\ &+ \{I(H_{k} = H_{1}^{\star}) + I(H_{l} = H_{1}^{\star})\}X_{1}\beta_{H_{1}^{\star}X_{1}}^{a} \\ &+ I(H_{k} = H_{l} = H_{1}^{\star})X_{1}\beta_{H_{1}^{\star}X_{1}}^{r} \end{split}$$

where $\boldsymbol{\gamma}_{H_1^{\star}} = (\beta_{H_1^{\star}}^a, \beta_{H_1^{\star}}^r, \beta_{H_1^{\star}X_1}^a, \beta_{H_1^{\star}X_1}^r)^{\top}$. Similarly,

• $\beta_{H_1^*}^r = \beta_{H_1^*X_1}^r = 0$ under the additive model; • $\beta_{H_1^*}^a = \beta_{H_1^*X_1}^a = 0$ under the recessive model; • $\beta_{H_1^*}^r = -\beta_{H_1^*}^a$ and $\beta_{H_1^*X_1}^r = -\beta_{H_1^*X_1}^a$ under the dominant model.

Example of including interaction of H_1^* with X_1 .

Subjects' diplotypes: $H_1^d = (000, 111)$, $H_2^d = (010, 100)$, $H_3^d = (010, 010)$ Risk haplotype H_1^\star : 010

Table: Expressions of $m\{H^d = (H_k, H_l), X_1; \gamma_{H_1^*}\}$ for different diplotypes under four genetic models.

	additive	dominant	recessive	codominant
$H_1^{\rm d}$	0	0	0	0
$H_2^{\overline{d}}$	$\beta^a_{H_1^\star} + \beta^a_{H_1^\star X_1} X_1$	$\beta^a_{H_1^\star} + \beta^a_{H_1^\star X_1} X_1$	0	$\beta^a_{H_1^{\star}}$
H_3^{d}	$2\beta_{H_1^{\star}}^a + 2\beta_{H_1^{\star}X_1}^a X_1$	$\beta_{H_1^{\star}}^a + \beta_{H_1^{\star}X_1}^a X_1$	$\beta_{H_1^{\star}}^r + \beta_{H_1^{\star}X_1}^r X_1$	$2\beta_{H_{1}^{\star}}^{a} + 2\beta_{H_{1}^{\star}X_{1}}^{a}X_{1} + \beta_{H_{1}^{\star}}^{r} + \beta_{H_{1}^{\star}X_{1}}^{r}X_{1}$



A haplotype-effects logistic regression model is

$$\Pr(D=1|X, H^{\mathrm{d}}; \alpha_0, \beta_X, \gamma_{H^*}) = \mathcal{K}(\alpha_0 + \beta_X^\top X + \gamma_{H^*}^\top M)$$

where components of a column vector M (genetic covariates) depend on subjects' diplotypes, chosen risk haplotypes H^* , the chosen mode of inheritance, and are evaluated using expressions described earlier for function $m(H^d, X; \gamma_{H^*})$.

How do we estimate the parameters of the above model? Let Z = (X, M) and $\beta = (\beta_X^{\top}, \gamma_{H^*}^{\top})^{\top}$ and follow Prentice and Pyke's approach as before.

So, are we done?

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- We have additional information about the distribution of covariates can still utilize the prospective approach but the results are no longer semiparametric-efficient.
- In practice, we usually observe genotypes instead of diplotypes "phase ambiguity" arises (will discuss later).
- Genotype data are often missing need to deal with the missing-data problem to avoid a possibly significant reduction in the sample size.



Additional information about covariate distribution

- gene-environment independence $f(X, H^d) = g(X)q(H^d; \theta)$
- population in Hardy-Weinberg equilibrium (HWE) assumption about the distribution of genetic covariates:

$$q\{H^{d} = (H_{k}, H_{l}); \boldsymbol{\theta}\} = \theta_{k}^{2} \quad \text{if } H_{k} = H_{l}$$
$$= 2\theta_{k}\theta_{l} \quad \text{if } H_{k} \neq H_{l}$$

where θ_k denotes the frequency for haplotype H_k .

• population deviates from HWE according to a certain parametric model. For example,

$$q\{H^{d} = (H_{k}, H_{l}); \theta\} = \theta_{k}^{2} + \rho \theta_{k} (1 - \theta_{k}) \quad \text{if } H_{k} = H_{l}$$
$$= (1 - \rho) \theta_{k} \theta_{l} \qquad \text{if } H_{k} \neq H_{l}$$

where ρ denotes the inbreeding coefficient.



What is phase ambiguity?

Recall, that we observe subjects' genotypes $G = H_k + H_l$ instead of diplotypes $H^d = (H_k, H_l)$. This creates a problem of "phase ambiguity" for heterozygous subjects who carry different alleles at two or more loci.

Definition

Homozygous subjects carry two copies of the same allele at all SNP loci. *Heterozygous subjects* carry different alleles at at least one locus.

Example

- 2 SNPs $H_1 = (0,0)$, $H_2 = (0,1)$, $H_3 = (1,0)$, and $H_4 = (1,1)$
- for a G = (1, 1) there are 2 diplotypes $\{H_1, H_4\}$ and $\{H_2, H_3\}$ consistent with it, i.e., $G = H_1 + H_4 = H_2 + H_3$
- for subjects with such genotype the phase is indeterminant

Genotype data G:

- missing at random;
- missing components of G may be any value from $\{0, 1, 2\}$.

Thus, for subjects with missing genotype data we take into account multiple possible genotypes (and consequently multiple possible diplotypes) when computing the likelihood.

Note

We can view the "phase ambiguity" problem as a missing-data problem.



Taking into account the discussed characteristics, the retrospective likelihood function of case-control ${\rm SNP}\xspace$ -based data is

$$\Pr(X = x, H^{\mathrm{d}} \in H^{\mathrm{d}}_{G} | D = d) = \frac{g(x) \sum_{h^{\mathrm{d}} \in H^{\mathrm{d}}_{G}} \Pr(D = d | X = x, H^{\mathrm{d}} = h^{\mathrm{d}}) q(h^{\mathrm{d}}; \theta)}{\Pr(D = d)}$$

where $H_G^d = \{(H_k, H_l):$ the haplotype pair is consistent with $G\}$ is the set of all possible diplotypes consistent with subject's genotype G.



Idea of the method: profile the possibly infinite-dimensional (if X has continuous components) nuisance distribution of X out of the retrospective likelihood first. Then maximize the resulting profile retrospective log-likelihood with respect to parameters of interest.

For details of the method and formulas, see Spinka et al. (2005), Lin et al. (2005), and Lin and Zeng (2006).



The retrospective sampling design is commonly used when conducting studies of rare diseases. Under the assumption of a rare disease,

$$\Pr(D = d \mid H^{\mathrm{d}}, X; \alpha_0, \beta_X, \gamma_{H^\star}) \approx \exp\{d(\alpha_0 + \beta_X^\top X + \gamma_{H^\star}^\top M)\}, \quad d = 0, 1$$

Lin and Zeng (2006) employed the rare-disease assumption for the development of their algorithm. Spinka et al. (2005) provided a method that does not make the assumption of a rare disease but noted that this assumption results in a simpler and more stable algorithm.



The Stata command haplologit estimates haplotype effects and haplotype-environment interactions from case-control genetic (SNP-based) data in the very important special case of

- a rare disease;
- a single candidate gene in HWE;
- independence of genetic and environmental factors.

haplologit accommodates three types of haplotype risk models: additive (the default), dominant, or recessive. It implements the retrospective profile-likelihood methods of Spinka et al. (2005) and Lin and Zeng (2006) which are equivalent under the assumptions of a rare disease and HWE.

For details about the syntax of haplologit, underlying algorithms, and examples see Marchenko et al. (2008).



Biological hypothesis

Calcium prevents colorectal cancer, possibly through the calcium-sensing receptor.

Study goal.

To investigate the interactions of dietary calcium intake and genetic variants in the calcium-sensing receptor (*CaSR*) region (Peters et al. 2004; Lobach et al. 2008; Chen et al. 2008).

Data source.

Data come from Prostate, Lung, Colorectal, and Ovarian Cancer Screening Trial at the National Cancer Institute, USA and contain information on participants' dietary food intake and genotype data from three nonsynonymous SNPs in the *CaSR* region.

SNP variables

Variables g_casr_01 , g_casr_02 , and g_casr_03 record genotype data from 3 nonsynonymous SNPs in exon 7 of the CaSR gene.

. describe g_casr_01 g_casr_02	g_casr_03 casecontrol	Ldtcal sex agerand Caucasian
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	storage	display	value	
variable name	type	format	label	variable label
g_casr_01	byte	%8.0g		first SNP locus
g_casr_02	byte	%8.0g		second SNP locus
g_casr_03	byte	%8.0g		third SNP locus
casecontrol	byte	%8.0g		case-control status
Ldtcal	float	%9.0g		log(1+dietary calcium from FFQ)
sex	byte	%8.0g		gender: 1 = Male, 2 = Female
agerand	float	%9.0g		age (in years)
Caucasian	float	%9.0g		ethnicity: 0 = Non Caucasian, 1
				= Caucasian

Total of 1312 subjects after eliminating subjects with missing calcium information – 644 cases and 668 controls.

Variable	Obs	Mean	Std. Dev.	Min	Max
g_casr_01	1312	.1623476	.3968026	0	2
g_casr_02	1312	.1021341	.3176886	0	2
g_casr_03	1312	.2804878	.4992599	0	2
casecontrol	1312	.4908537	.500107	0	1
Ldtcal	1312	6.767107	.506731	4.893262	8.544137
sex	1312	1.304878	.4605313	1	2
agerand	1312	62.53329	5.276247	55.042	74.99
Caucasian	1312	.9458841	.2263324	0	1

. summarize g_casr_01 g_casr_02 g_casr_03 casecontrol Ldtcal sex agerand Caucasian



Example

We want to investigate the interaction of dietary calcium intake (mg/day) and the three common haplotypes coded as "001", "010", and "100". Other rare haplotypes are combined with the most common haplotype, "000", to form the base (comparison) haplotype category.

Syntax

- . haplologit casecontrol sex Ldtcal agerand Caucasian,
- > snpvars(g_casr_01 g_casr_02 g_casr_03) inher(d)
- > riskhap1("001") riskhap2("010", inter(Ldtcal))
- > riskhap3("100", inter(Ldtcal))
- > nolog happrefix("_")

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Building consistent haplotype pairs:

Obtaining initial haplotype frequency estimates from the control sample:

Haplotype frequency EM estimation

Number of iterations = 53 Sample log-likelihood = -982.17816

haplotype	frequency*		
000 001	.71033		
010 100	.055389		

* frequencies > .0015244

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Output – haplotype-effects estimation

Performing gradient-based optimization:			
Haplotype-effects logistic regression Mode of inheritance: dominant	Number of obs	=	1312
Genetic distribution: Hardy-Weinberg equilib.	Number phased	=	1253
Genotype: g_casr_01 g_casr_02	Number unphased	=	59
g_casr_03	Number missing	=	0
	Wald chi2(9)	=	36.61

Retrosp. profile log likelihood = -2769.5997 Prob > chi2

casecontrol	Coef.	Std. Err.	z	P> z	[95% Conf.	Interval]
sex	1222521	. 12261	-1.00	0.319	3625632	.118059
Ldtcal	0553412	.1213515	-0.46	0.648	2931857	.1825032
agerand	.0370709	.0105986	3.50	0.000	.016298	.0578439
Caucasian	.1579015	.2517616	0.63	0.531	3355422	.6513452
_001	2915038	.1238556	-2.35	0.019	5342563	0487513
_010	4371039	.1932946	-2.26	0.024	8159544	0582533
_100	2507072	.1535909	-1.63	0.103	5517398	.0503254
_010*Ldtcal	7947331	.2759949	-2.88	0.004	-1.335673	253793
_100*Ldtcal	5047162	.2205877	-2.29	0.022	9370601	0723723
_cons	.1193802	.2939819	0.41	0.685	4568137	.6955741

Note: _cons = b0 + ln(N1/N0) - ln{Pr(D=1)/Pr(D=0)}

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Yulia Marchenko (StataCorp)

Haplotype-based disease association analysis

0.0000

=

Haplotype frequencies

[95% Conf. Interval]	
.7	267127
.91 .1	713713
. 46	070218
.31 .1	.012729
46 71	4646 . 7131 .1



Results

• haplotype main effects

significant dominant effects of "001" and "010" haplotypes

environmental factors

significant findings – age is associated with an increased risk of the disease;

nonsignificant findings – an increased risk of advanced colorectal adenoma for Caucasians, males, and subjects with lower calcium intake

haplotype-environment interactions

Both interaction terms, hap_010*Ldtcal and hap_100*Ldtcal, are statistically significant at the 1% and 5% levels, respectively. This agrees with results obtained in Lobach et al. (2008).



- allow modeling of departures from HWE according to a number of specific models as described in Lin and Zeng (2006)
- weaken the gene-environment independence assumption (e.g. Cheng et al. 2008)
- complete the list of genetic models by adding a codominant model
- allow multiple candidate genes and gene-gene interactions
- allow population stratification
- handle large number of markers important in genome-wide association studies



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Consultants.

Raymond J. Carroll is a distinguished professor of statistics, nutrition, and toxicology at Texas A&M University.

Danyu Lin is a Dennis Gillings distinguished professor of biostatistics at the University of North Carolina.

Christopher I. Amos is a professor of epidemiology at the M. D. Anderson Cancer Research Center.



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